Problem 34)

$$f(z) = f(x+iy) = (x-y)^2 + 2i(x+y)$$
.

$$U(x,y) = (x-y)^2$$
, $2^y(x,y) = 2(x+y)$

Cauchy-Riemann Conditions:

$$\frac{\partial u}{\partial n} = 2(n-y); \quad \frac{\partial u}{\partial y} = -2(n-y); \quad \frac{\partial v}{\partial n} = 2; \quad \frac{\partial v}{\partial y} = 2.$$

$$\int \frac{\partial u}{\partial x} = \frac{\partial^2 u}{\partial y} = \int 2(x-y) = 2 = \int x-y = 1.$$

$$\left(\frac{\partial u}{\partial y} = -\frac{\partial z^2}{\partial x} \Rightarrow\right) - 2(x-y) = -2 \Rightarrow x-y=1.$$

Clearly, the straight-line n-y=1 is the only place with the Co-plex-plane Z where the function f(2) is differebiable.

At no point on the straight—line x-y=1 can we find a small neighborhood (i.e., a Small Cicle Centered at that point) when the function is differentiable energwhere with the neighborhood. Therefore f121 is analytic at no point.